

# WATKINS-JOHNSON TOPOLOGY INTEGRATED IN A FULL-BRIDGE CONVERTER

Giulio Simonelli  
Oliver Korashy  
Hadrien Carbonnier  
Los Angeles  
04/26/2018

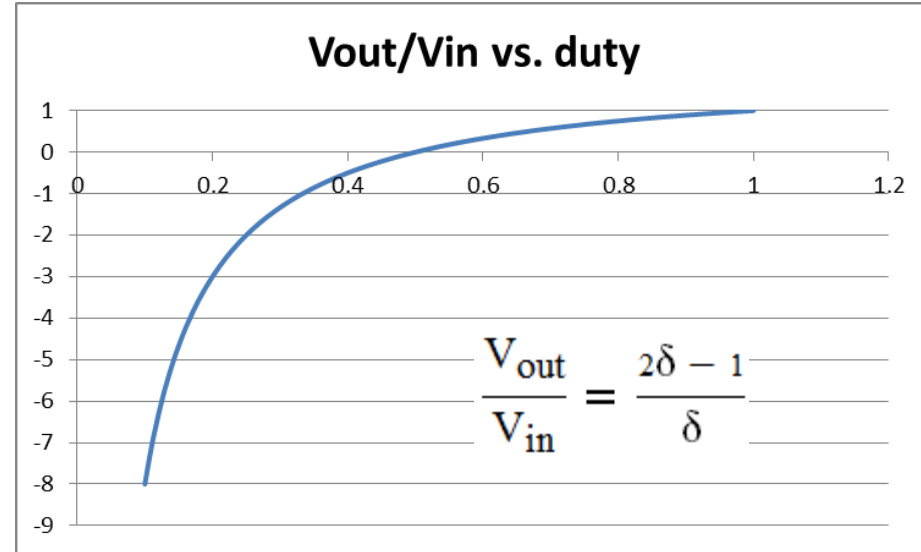
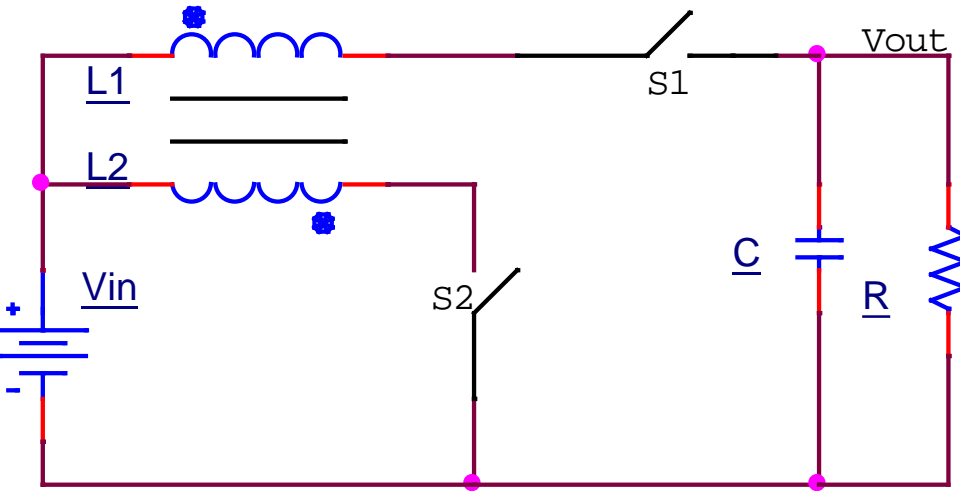
ESA UNCLASSIFIED – Releasable to the Public

ESA UNCLASSIFIED - Releasable to the Public

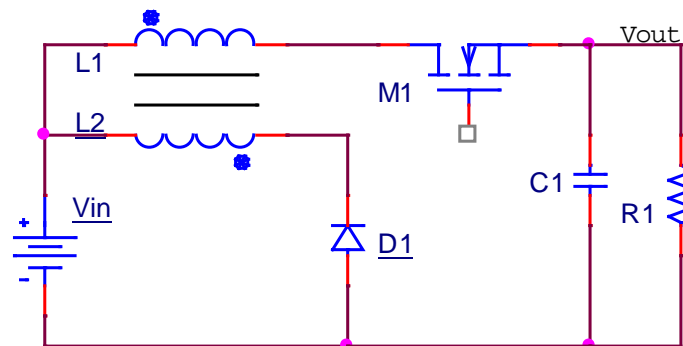


1. The Watkins-Johnson topology
2. Watkins-Johnson topology integrated in a Full-Bridge
3. Operations
4. Continuous Current Mode
5. Test results
6. Circuit Equivalent Modelling
7. Discontinuous Current Mode
8. Advantages (and disadvantages)
9. Further Work

# The Watkins-Johnson topology: basic

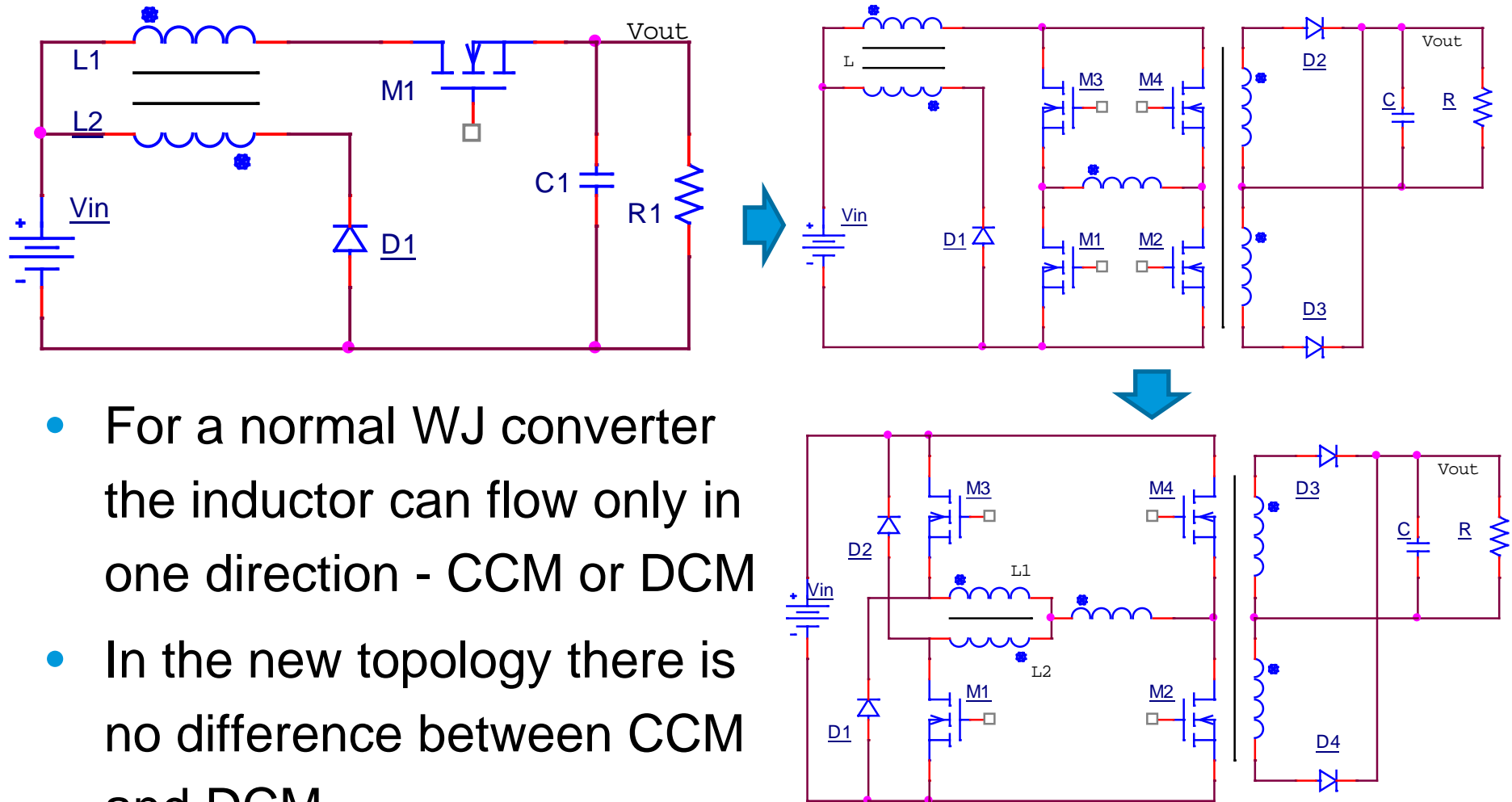


Basic topology with bidirectional switches and the related transfer ratio



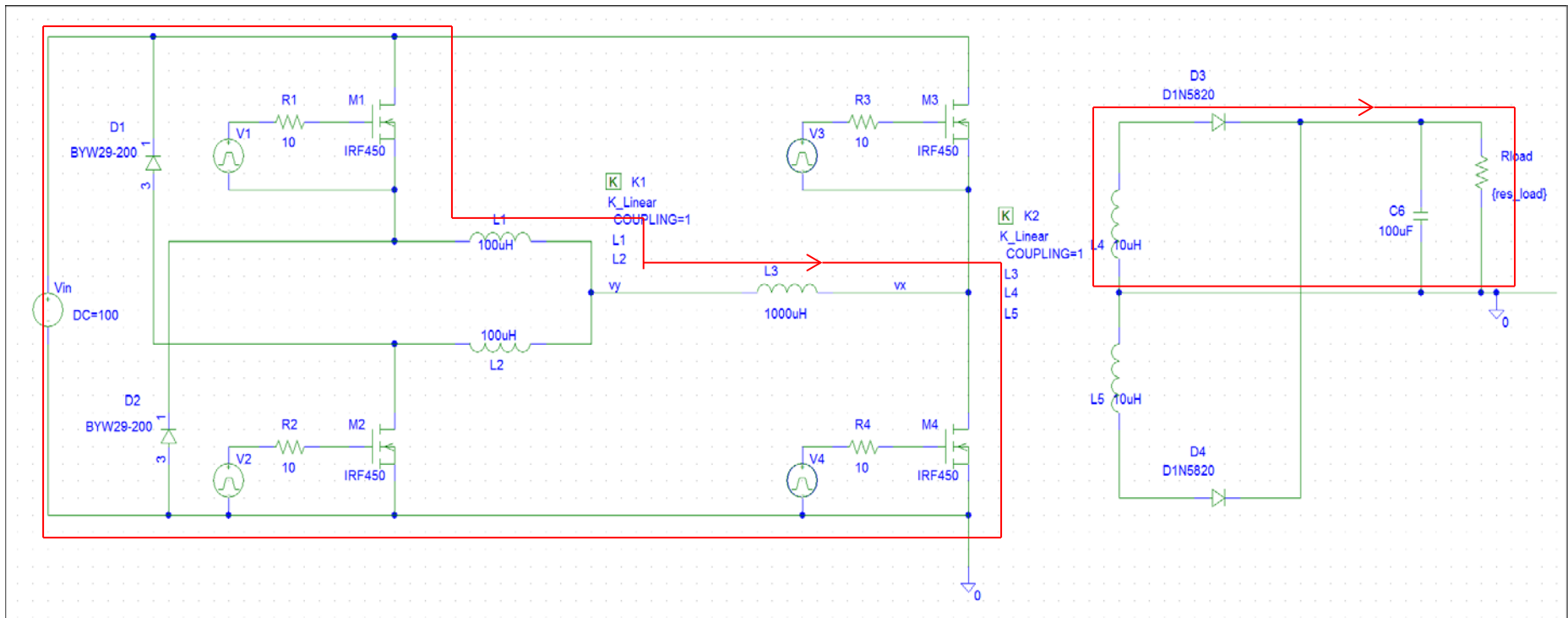
Practical realization with MOSFET and diode

# Topology integration in a Full-Bridge

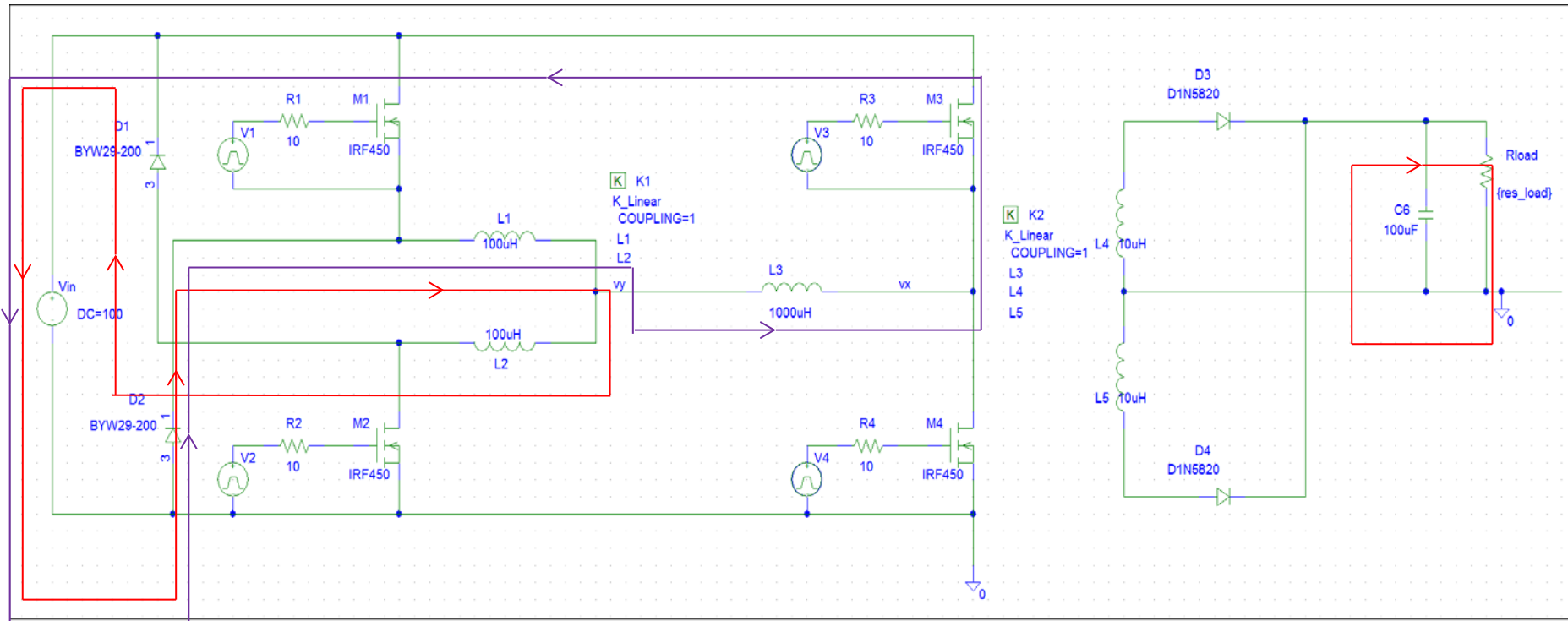


- For a normal WJ converter the inductor can flow only in one direction - CCM or DCM
- In the new topology there is no difference between CCM and DCM

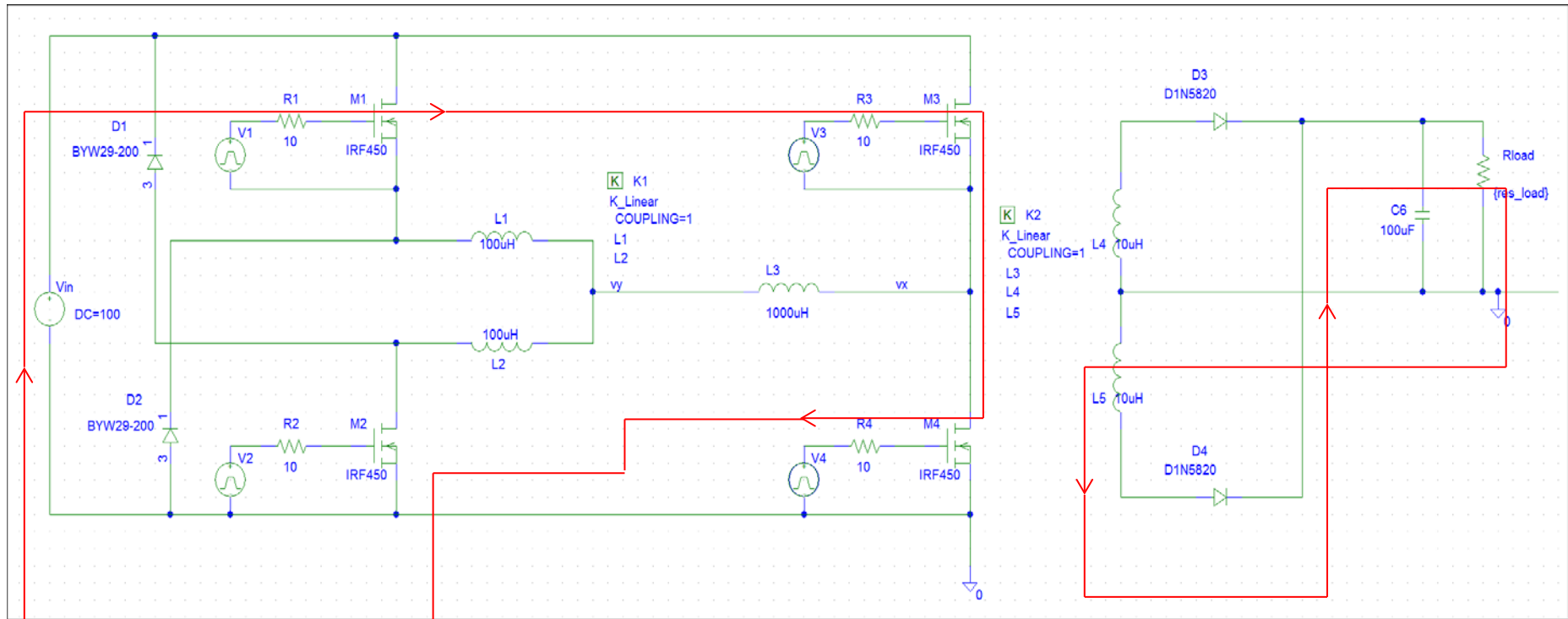
# Operation: from T0 to T1 (On Time)



# Operation: from T1 to T2 (Off Time)

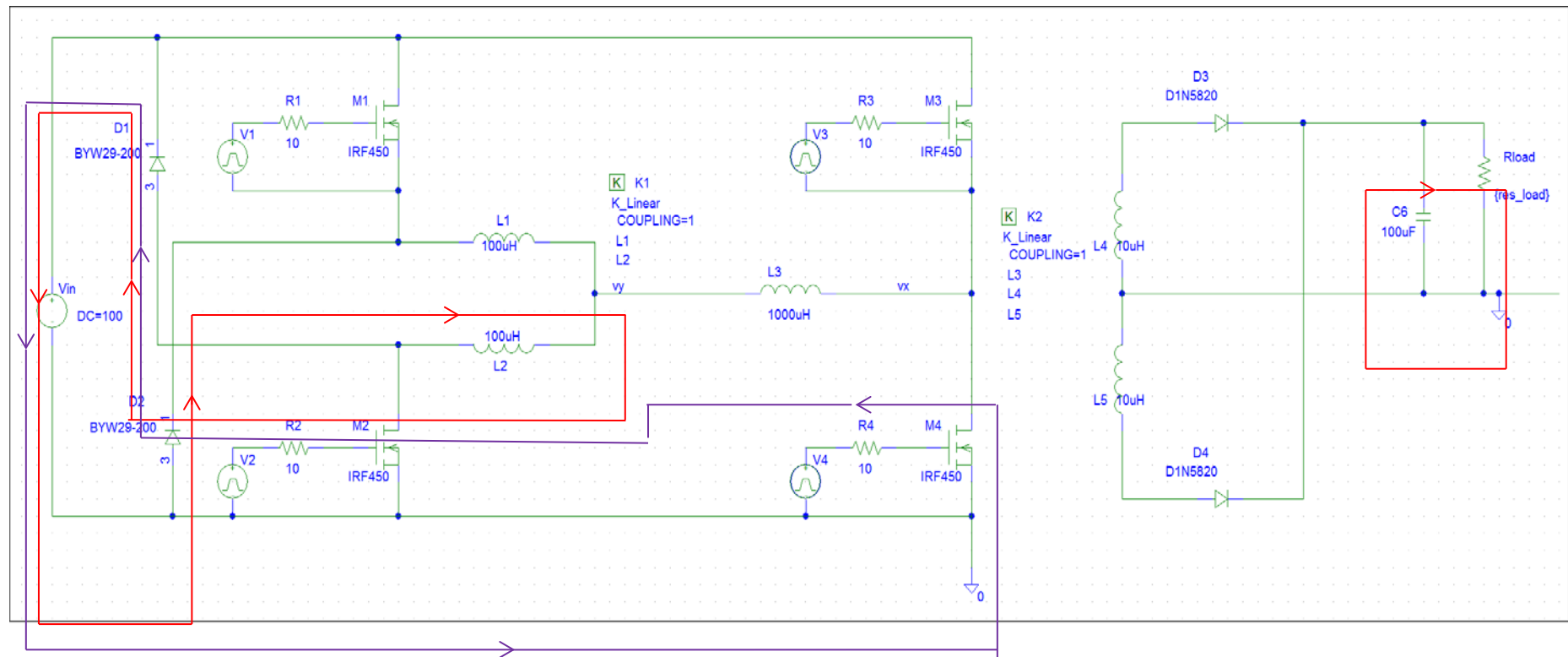


# Operation: from T2 to T3 (On Time)



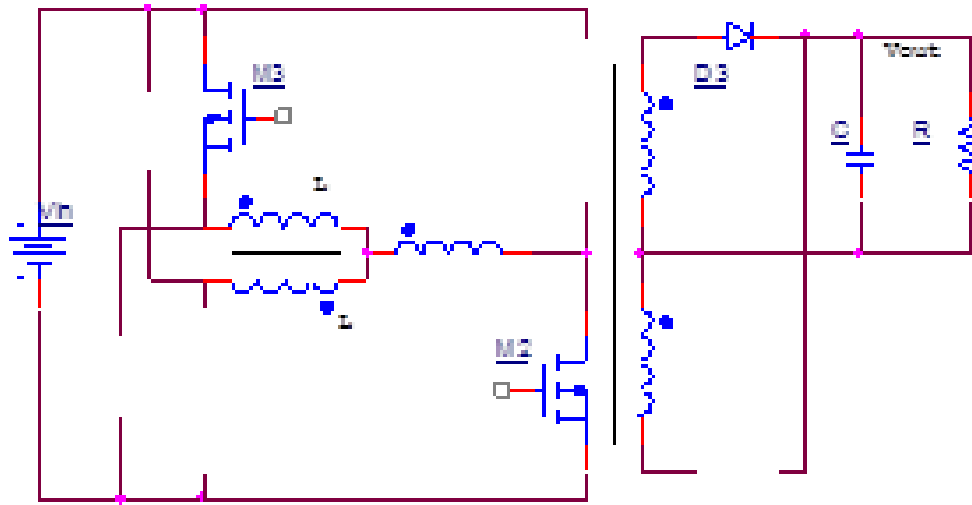


# Operation: from T3 to T4 (Off Time)





# Continuous Current Mode: governing equations during On Time



$i_{on}$ : is the current in the inductance during on time  
 $n$ : is the transformer ratio  $N_p/N_s$   
 $R_L$ : is parasitic resistance of  $L$   
 $R_C$ : is the ESR of  $C$   
 $R$ : is the Resistive Load

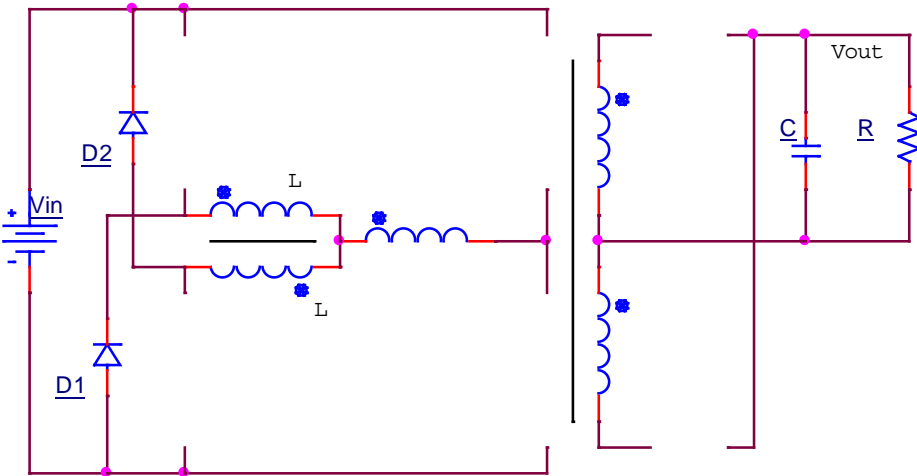
$$L \cdot \frac{d}{dt} i_{on} = v_{in} - R_L \cdot i_{on} - n \cdot (v_{out} + V_{ds})$$

$$C \cdot \frac{d}{dt} v_c = n \cdot i_{on} - \frac{v_{out}}{R}$$

$$v_{out} = v_c + R_c \cdot i_c$$

$$i_{in} = i_{on}$$

# Continuous Current Mode: governing equations during Off Time



$$L_{12} \cdot \frac{d}{dt} i_{\text{off}} = -2 \cdot R_L \cdot i_{\text{off}} - 2V_{\text{dp}} - v_{\text{in}}$$

$$C \cdot \frac{d}{dt} v_c = \frac{-V_{\text{out}}}{R}$$

$$i_{\text{in}} = -\frac{i_{\text{on}}}{2}$$

$$V_{\text{out}} = v_c + R_c \cdot i_c$$

$L_{12}$  is the inductance of the 2 mutual inductance in series

$I_{\text{off}}$  is the current in the inductance during off time

$R_L$  is parasitic resistance of L

$R_C$  is the ESR of C

R is the Resistive Load

# Continuous Current Mode: averaging of the governing equations

Considering that  $L_{12}=4 \cdot L$  and that  $i_{\text{off}} = i_{\text{on}}/2$  the Off phase inductor equation become:

$$4 \cdot L \cdot \frac{d}{dt} \frac{i_{\text{on}}}{2} = -2 \cdot R_L \cdot \frac{i_{\text{on}}}{2} - 2V_{\text{dp}} - V_{\text{in}}$$

Rearranging for the Off phase we have

$$L \cdot \frac{d}{dt} i_{\text{on}} = -R_L \cdot \frac{i_{\text{on}}}{2} - V_{\text{dp}} - \frac{V_{\text{in}}}{2}$$

# Continuous Current Mode: averaging of the governing equations

$$L \cdot \frac{d}{dt} i_{on} = v_{in} - R_L \cdot i_{on} - n \cdot (v_{out} + V_{ds})$$

$$C \cdot \frac{d}{dt} v_c = n \cdot i_{on} - \frac{v_{out}}{R}$$

$$v_{out} = v_c + R_c \cdot i_c$$

$$i_{in} = i_{on}$$

ON

$$L \cdot \frac{d}{dt} i_{on} = -R_L \cdot \frac{i_{on}}{2} - V_{dp} - \frac{v_{in}}{2}$$

$$C \cdot \frac{d}{dt} v_c = \frac{-v_{out}}{R}$$

$$v_{out} = v_c + R_c \cdot i_c$$

$$i_{in} = -\frac{i_{on}}{2}$$

OFF

$$L \cdot \left( \frac{d}{dt} i_{avg} \right) = \left( \frac{3 \cdot \delta}{2} - \frac{1}{2} \right) \cdot v_{in\_avg} - \frac{(\delta + 1) \cdot R_L}{2} \cdot i_{on\_avg} - (1 - \delta) \cdot V_{dp} - \delta \cdot n \cdot V_{ds} - \delta \cdot n \cdot v_{out\_avg}$$

$$C \cdot \left( \frac{d}{dt} v_{c\_avg} \right) = \delta \cdot n \cdot i_{avg} - \frac{v_{out\_avg}}{R}$$

$$v_{out\_avg} = v_{c\_avg} + R_c \cdot i_{c\_avg}$$

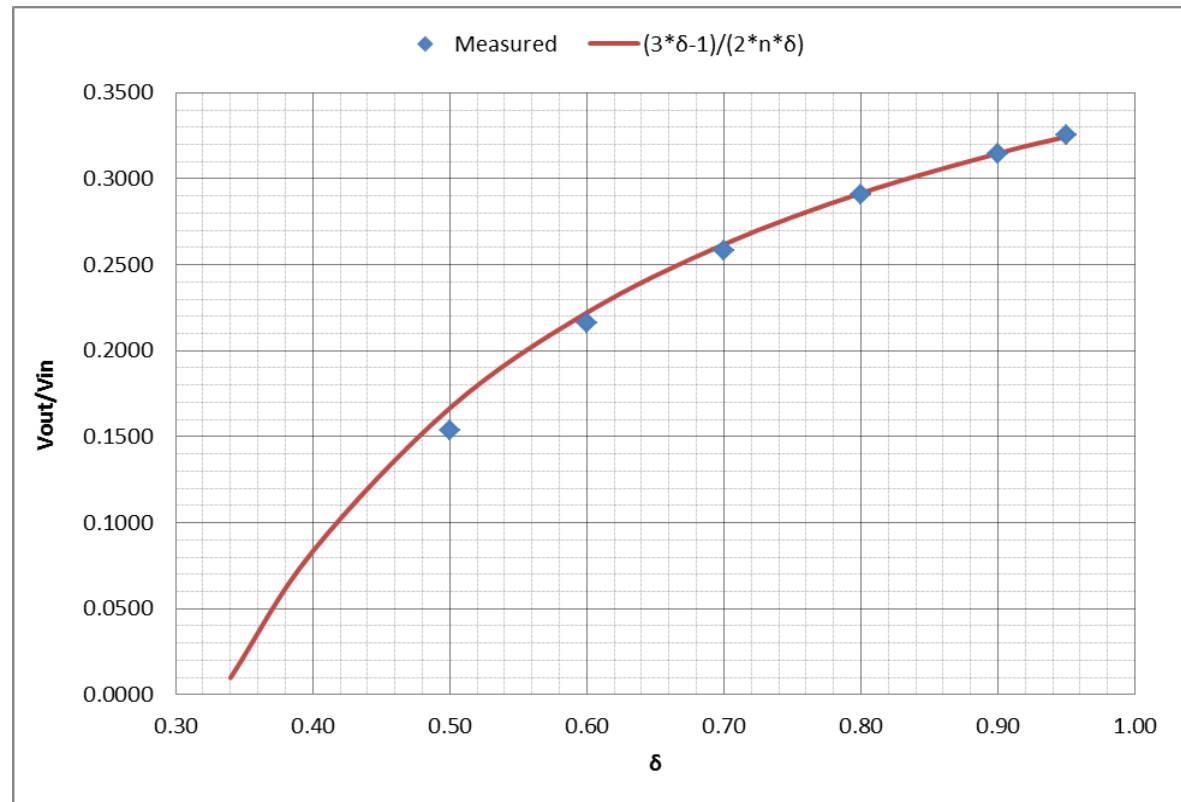
$$i_{in\_avg} = \left( \frac{3 \cdot \delta}{2} - \frac{1}{2} \right) \cdot i_{avg}$$

AVERAGE

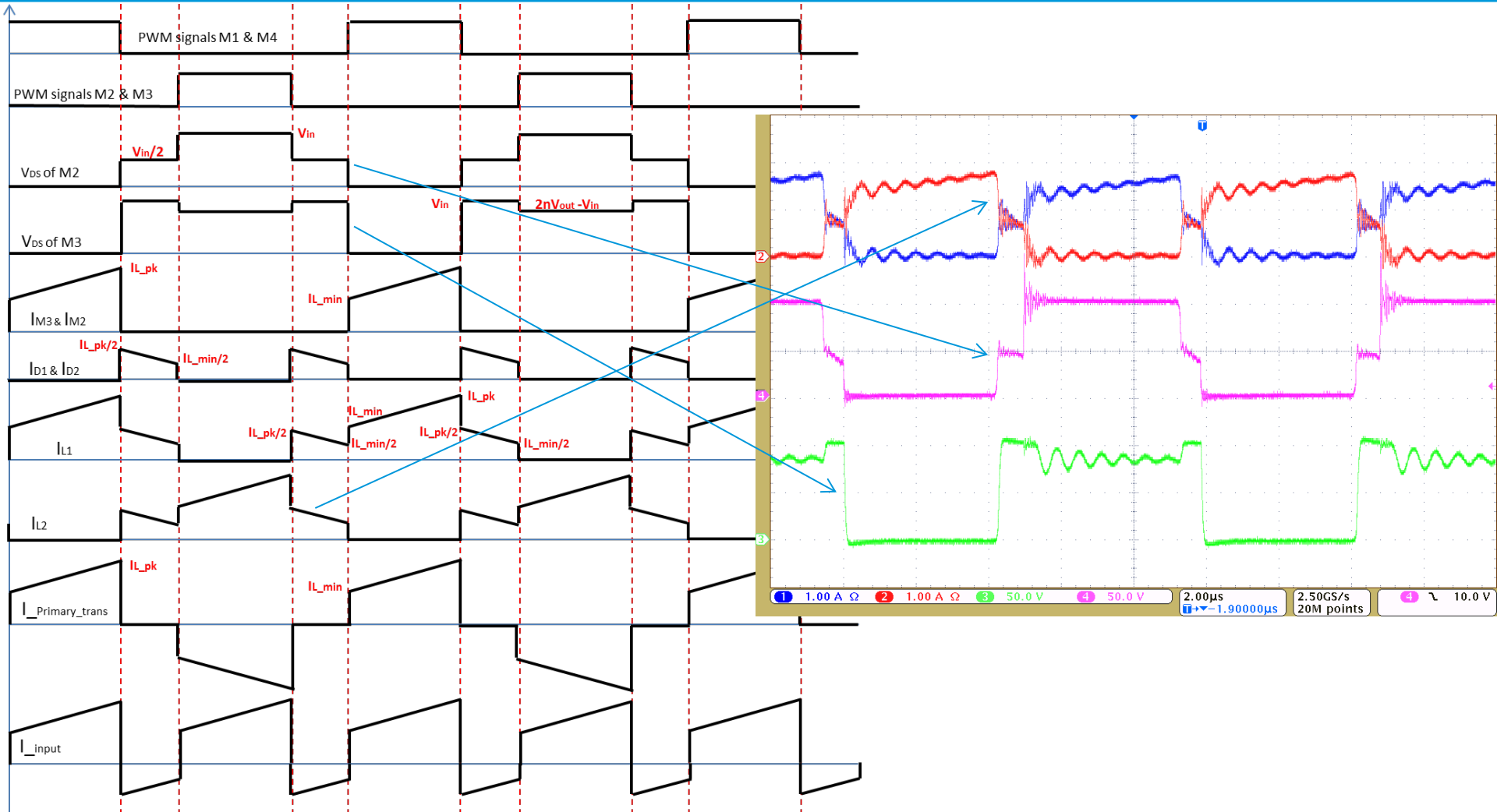
# Continuous Current Mode: Test results in DC

The DC case is described by the previous equations imposing the derivative equal to zero. From the inductor equation and considering an ideal converter we find the transfer ratio of the converter is:

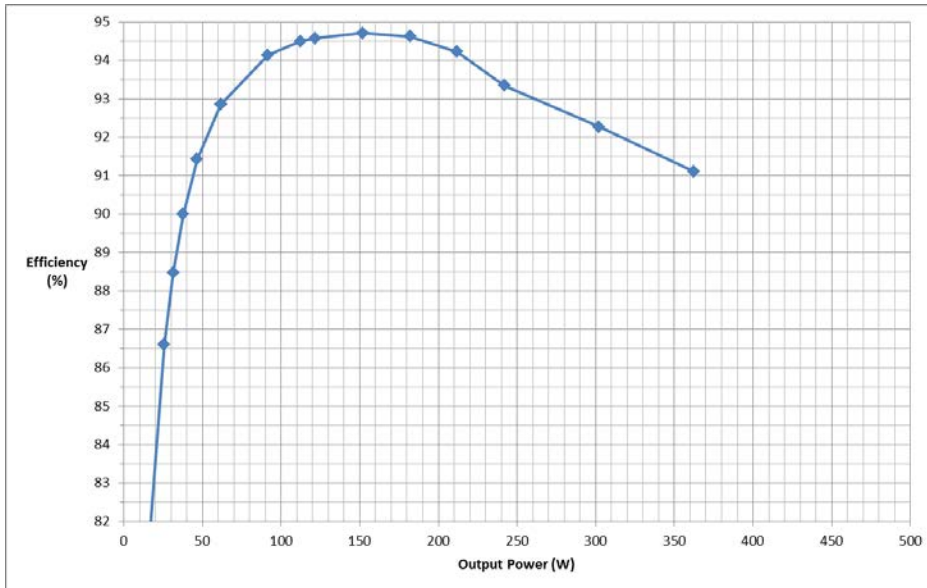
$$\frac{V_{out}}{V_{in}} = \frac{3 \cdot \delta - 1}{n \cdot 2 \cdot \delta}$$



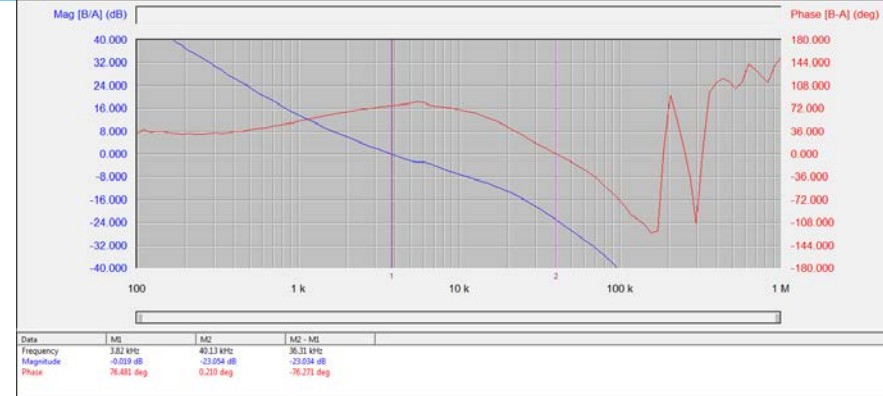
# Continuous Current Mode: measured main waveforms



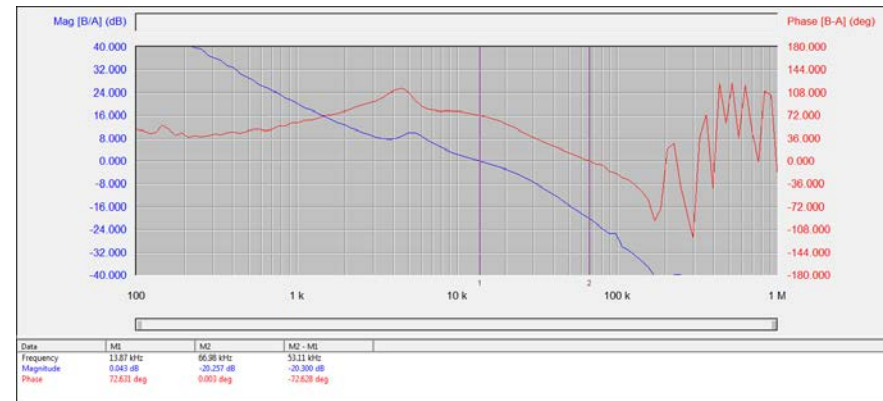
# Continuous Current Mode: efficiency and stability measurements



Without much optimization effort the efficiency of the BB is >92% up to 300W.



10W & 200W load:  
 $G_{margin} > 10\text{dB}$ ,  
 $F_{margin} > 60\text{deg}$





# Simulation Model of the Converter in CCM

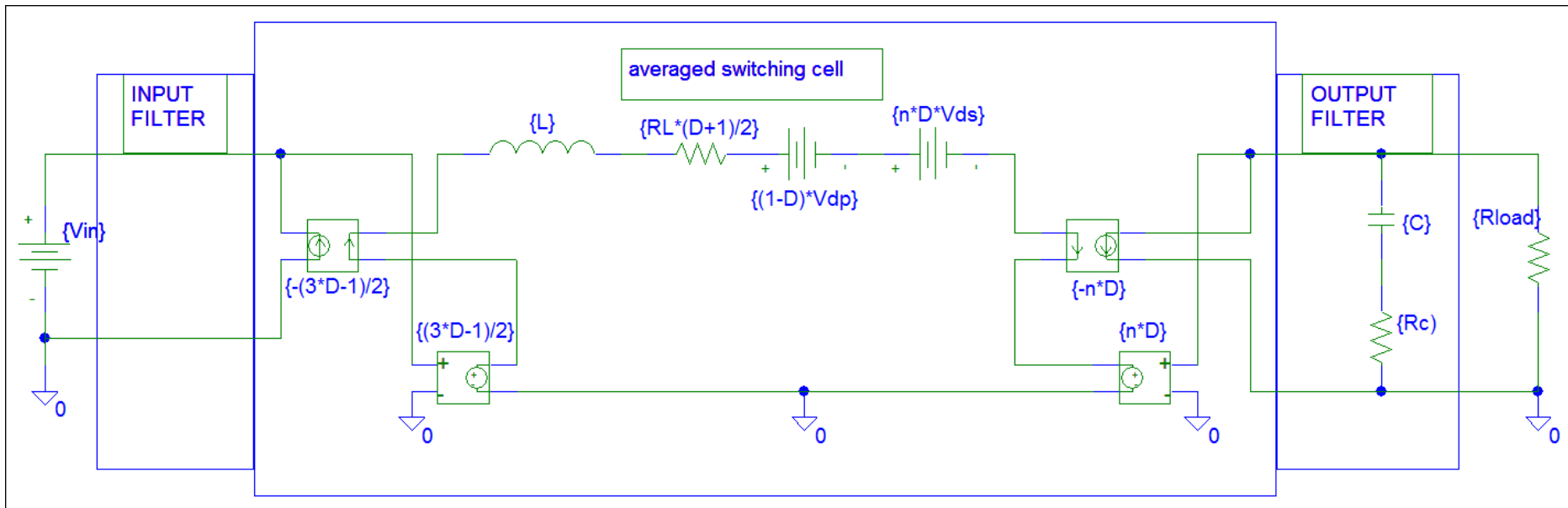
$$L \cdot \left( \frac{d}{dt} i_{avg} \right) = \left( \frac{3 \cdot \delta}{2} - \frac{1}{2} \right) \cdot v_{in\_avg} - \frac{(\delta + 1) \cdot R_L}{2} \cdot i_{on\_avg} - (1 - \delta) \cdot V_{dp} - \delta \cdot n \cdot V_{ds} - \delta \cdot n \cdot v_{out\_avg}$$

$$C \cdot \left( \frac{d}{dt} v_{c\_avg} \right) = \delta \cdot n \cdot i_{avg} - \frac{v_{out\_avg}}{R}$$

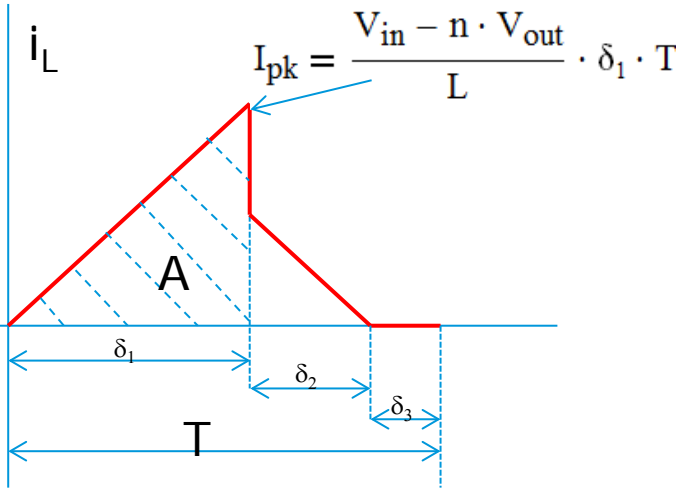
$$v_{out\_avg} = v_{c\_avg} + R_c \cdot i_{c\_avg}$$

$$i_{in\_avg} = \left( \frac{3 \cdot \delta}{2} - \frac{1}{2} \right) \cdot i_{avg}$$

AVERAGE



# Discontinuous Current Mode: Transfer Ratio



$$I_{L\_avg\_on} = \frac{1}{n} \cdot \frac{V_{out}}{R}$$

But also:

$$I_{L\_avg\_on} = \frac{A}{T} = \frac{V_{in} - n \cdot V_{out}}{L} \cdot \delta_1 \cdot \delta_1 \cdot T$$

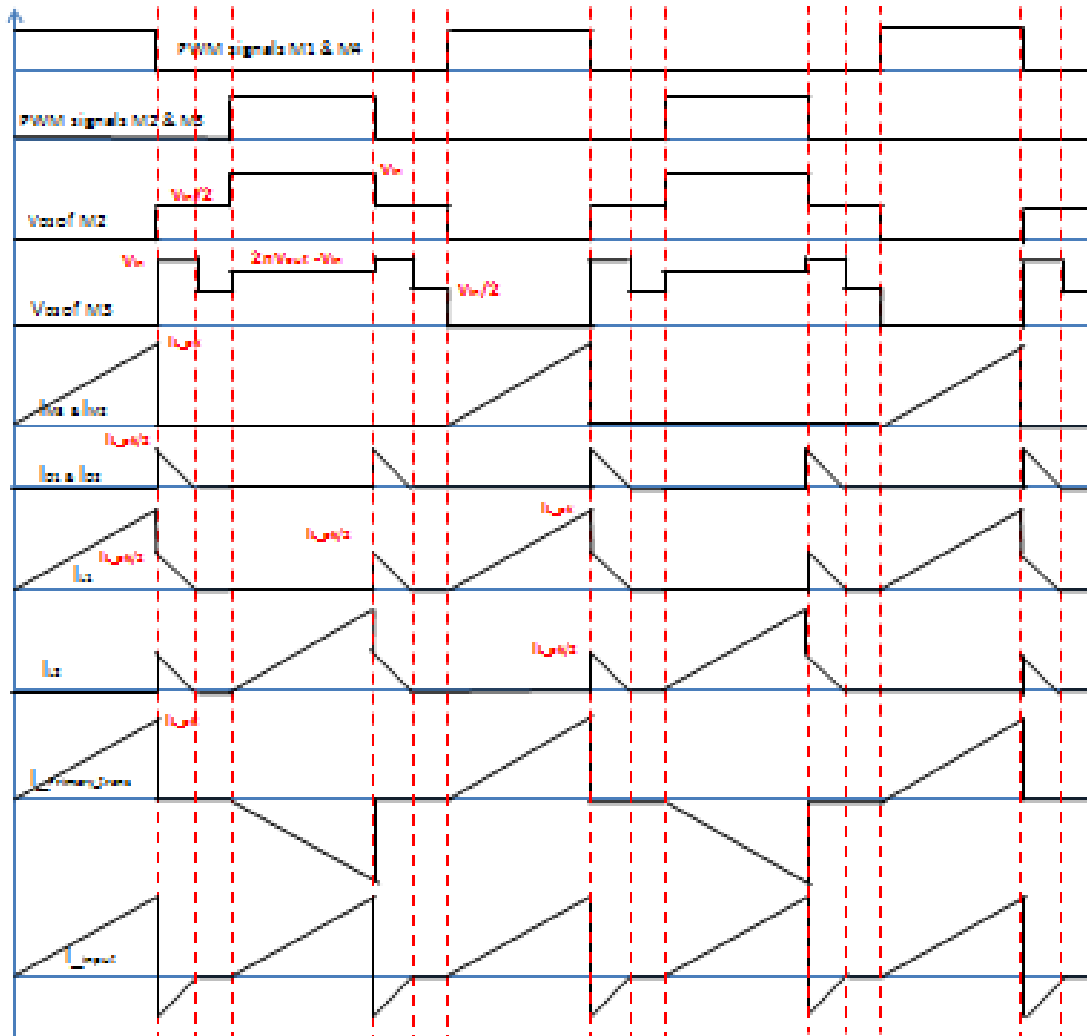
Eliminating  $I_{L\_avg\_on}$  from the two equations:

$$\frac{V_{out}}{V_{in}} = \frac{\delta^2}{n \cdot (K + \delta^2)}$$

Where:

$$K = \frac{2 \cdot L}{n^2 \cdot R \cdot T}$$

# Discontinuous Current Mode: main waveforms



# CCM and DCM boundary conditions



The boundary condition is a function of the duty cycle/

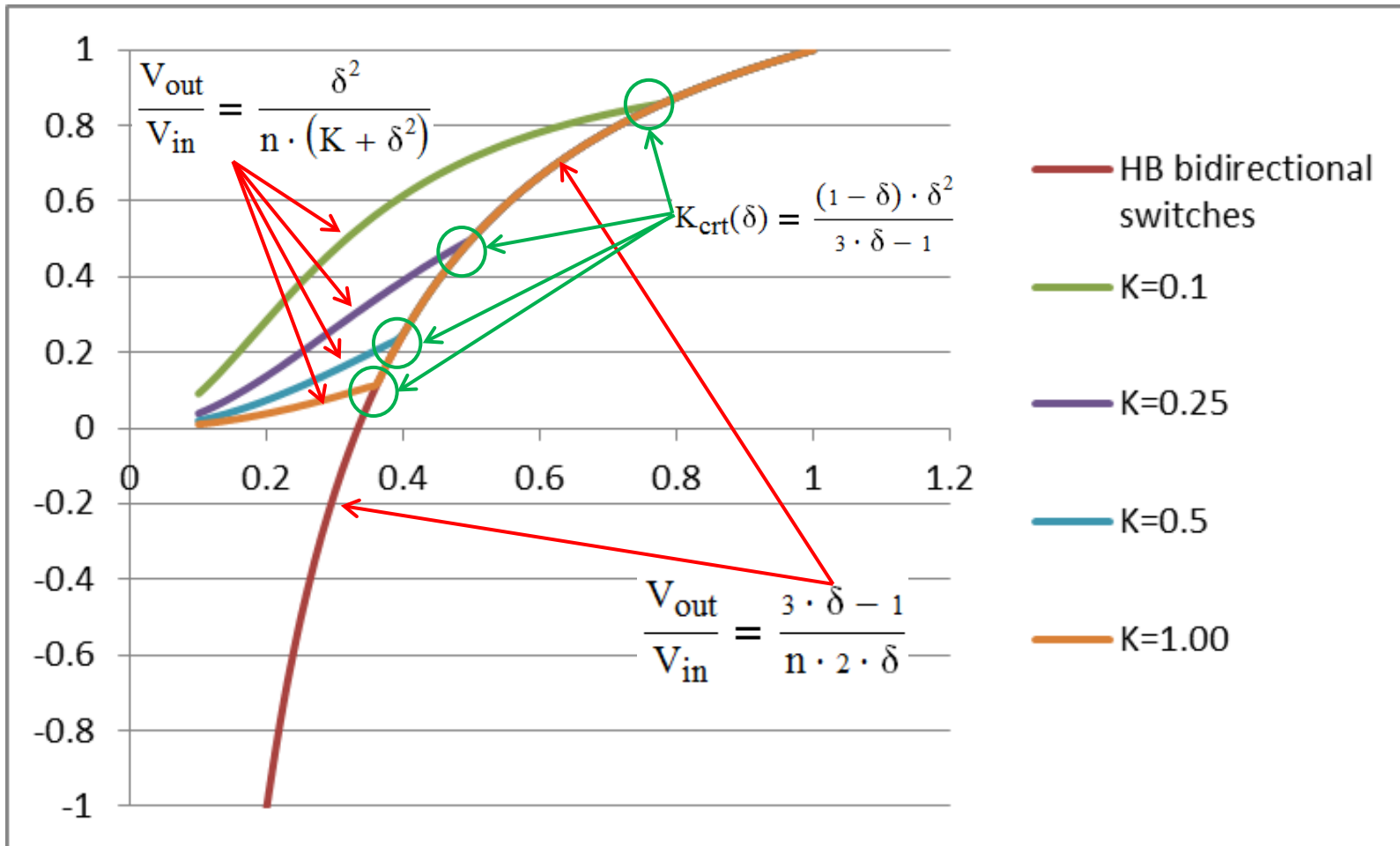
$$K_{\text{crt}}(\delta) = \frac{(1 - \delta) \cdot \delta^2}{3 \cdot \delta - 1}$$

If:  $K = \frac{2 \cdot L}{n^2 \cdot R \cdot T} > K_{\text{crt}}(\delta)$  the converter is in CCM

If:  $K = \frac{2 \cdot L}{n^2 \cdot R \cdot T} < K_{\text{crt}}(\delta)$  the converter is in DCM

So for high values of K (high loads) the converter will be in CCM for most of the duty-cycle domain range. For  $K = \infty$  (output in short circuit) the converter will be always in CCM and when duty  $< 1/3$  the output is 0V.

# Converter Transfer Ratio in CCM and DCM



# Advantages and Disadvantages of the topology

## Advantages:

- **Low voltage stress on switches:** maximum static voltage on the active components is  $V_{in}$ , while in the classical Watkins-Johnson converter the Voltage stress is  $2 \cdot V_{in}$ .
- **Simple output stage:** No inductance on the secondary side, hence topology suitable for HV applications.
- **Galvanic isolation**
- **High power handling capability:** topology suitable for high power applications due to the Full Bridge stage.

# Advantages and Disadvantages of the topology

## Advantages:

- **Operation possible in a wide input voltage range**
- **Stable:** easy to implement a stable control loop
- **Simple controller:** a simple PWM controller do the job
- **No uncontrolled overvoltage failure:** at maximum duty-cycle  $V_{out}=V_{in}/n$

## Disadvantages:

- **Alternating input current**



- Study control loop stability in detail
- Study the effect of the “parasitics” of the inductor and of the transformer
- Efficiency optimization, also finding conditions for partial ZVS operations
- Study how to achieve full ZVS operations
- Implement HV output stage
- Develop a modular approach to increase output power

# Questions or comments?

